

Activity 29

Brown Academy

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 Summer Urban Institute, Urban IMPACT Project



Description of Module

In designing this module, several areas of Brown Academy will be visited. The participant will solve mathematics problems based on data collected in the cafeteria, in the gymnasium, in the library, in the hallway, on the staircases, in the parking lot, and on the exterior of the building. Location: 718 E. 8th St., Chattanooga, TN 37403

Standards

Number and Operations, grades 6-12	Algebra, grades 6-12
Geometry, grades 6-12	Measurement, grades 6-12
Data Analysis and Probability, grades 6-12	Connections, grades 6-12

Standards Documents

National Council of Teachers of Mathematics. (2000). *Principles and standards for school mathematics*. Retrieved July 17, 2003, from <http://standards.nctm.org>

National Council of Teachers of Mathematics. (2003). *Illuminations*. Retrieved July 17, 2003, from <http://illuminations.nctm.org/>

Tennessee Department of Education. (2002). *Mathematics curriculum standards*. Retrieved July 17, 2003, from <http://www.state.tn.us/education/ci/cistandards2001/math/cimath.htm>

Hamilton County Department of Education. (2002). *HCDE standards & benchmarks*. Retrieved July 17, 2003, from <http://www.hcde.org/standards/stindex.html>

Problems

Part 1: Library

1. The bookshelf that holds Encyclopedia Britannica is 35 inches wide. Each volume of the encyclopedia is $1\frac{1}{2}$ inches wide (across the binding). The bottom shelf contains 22 volumes. Is there space for additional volumes? If so, how many?
2. The fiction books range in height from 7 inches to 11 inches. The bookcase that contains fiction is 54 inches tall. There are 39 shelving holes with $1\frac{1}{4}$ -inch spacing between them. The shelf is $\frac{3}{4}$ -inch thick. Design an arrangement for the shelving.
3. The width (across the binding) of fiction books ranges from $\frac{1}{2}$ inch to 1 inch. The bookshelf is 35 inches wide. What is the minimum number of books that will fill the shelf? What is the maximum number of books that will fill the shelf?
4. The magazine rack tilts to display the cover of the latest issue of each magazine. What is the slope of the tilted surface if the depth of the case is 1 foot and the height of the case is 10 inches?
5. The library contains square tables and round tables. Each square table has sides of length 42 inches. Each round table has a diameter of 41 inches. Find the surface area of each type of table.

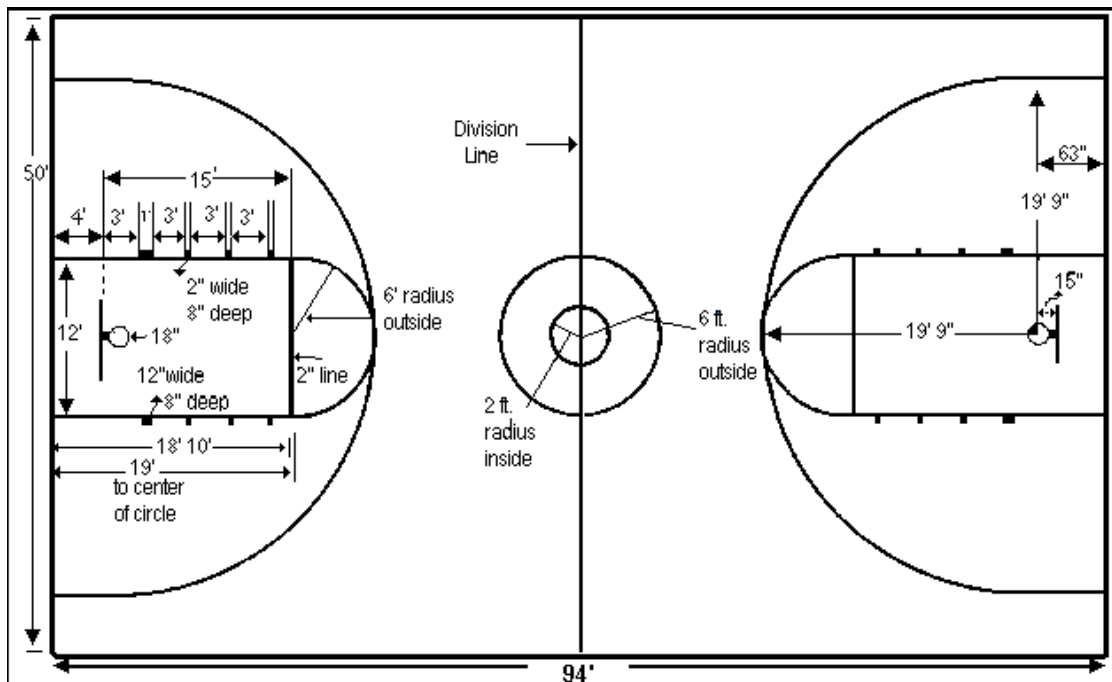
Part 2: Gymnasium

6. The gymnasium floor contains markings for a basketball court. Describe the lines, angles, and symmetry that can be seen.
7. Given the full court (NBA/NCAA) diagram (Handymanwire, 2003), find the following:
 - a. The ratio of the length of the court (94 ft) to the width of the court (50 ft).
 - b. The area of the backboard (72 inches in width by 42 inches in height).
 - c. The area of the key (12 ft wide, 15 ft from free throw line to backboard, 4 ft from backboard to baseline). Don't forget the semicircle at the top of the key!
 - d. The area of the rim (18 inches in diameter).
 - e. The circumference of the rim (18 inches in diameter).
 - f. The circumference of an NBA basketball is 29.5 inches. How many inches clearance does the basketball have as it passes through the rim?
 - g. The volume of an NBA basketball.

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- h. The length of the hypotenuse of the right triangle formed by the distance from the free throw line to the backboard (15 ft) and the distance from the floor to the rim of the basket (10 ft).



Part 3: Cafeteria

8. The wall is composed of 8-inch blocks. Find the height of the wall.
9. Each cafeteria table has a length of $95 \frac{1}{2}$ inches, a table width of $14 \frac{1}{2}$ inches, and a bench width of $11 \frac{1}{2}$ inches. Find the surface area of the table and the bench (top surface only).
10. Estimate the following:
 - a. The number of adults that can sit side-by-side on the bench.
 - b. The number of students that can sit side-by-side on the bench.
 - c. If there are 45 tables, how many students can be seated at the same time?
11. Count the number of 1-foot tiles along the length and width of the floor. Calculate the area of the floor in square feet and in square yards. Consider only full tiles.

12. Count the number of 4-foot by 2-foot panels along the length and width of the ceiling. Calculate the area of the ceiling in square feet and in square yards. Consider only full panels.
13. Compare the results obtained in problems 11 and 12 by calculating the percent error between the two measurements. Both values are based on observations, but the length as counted in floor tiles will be more accurate since this is a smaller unit. Use the area calculated with floor tiles as the accepted value and the area calculated with ceiling panels as the observed value.
14. Using the data collected in problems 8 and 11, calculate the volume of the room. Count the number of 2-foot diffusers and the number of 2-foot by 1-foot uptake vents in the ceiling. What volume of air is changed per diffuser and per uptake vent? Assume two room changes of air per hour. Express your answers in cubic feet per minute (cfm).
15. Count the number of 4-foot by 2-foot light panels in the ceiling. Calculate the percentage of the ceiling that has light panels.
16. Count the number of sprinkler heads in the ceiling. Calculate the percentage of the ceiling panels that contain a sprinkler head.
17. Draw a scale of the room. Construct the minimum size of the sprinkler head spray radius to obtain complete coverage of the floor.
18. Locate a nine-pane window. How many different sizes of panes are present? What is the ratio of the smallest pane to the largest pane?

Part 4: Connections

19. Look for patterns in the hallway and/or room floor tiles, on the walls, etc. Where can you find examples of odd numbers, even numbers, and/or prime numbers?
20. Look at the murals in the hallway, across from the school office. List the following:
 - a. Geometric shapes that you see.
 - b. Repeated patterns that you see.
 - c. Types of symmetry that you see.
 - d. List the time periods and locations that you see.

21. Look at the left or right side of the roof of the Tennessee Aquarium model. Measure the three sides of the large and small triangles. Show that they are similar.
22. Measure the height of the knight sculpture. What percentage of your height is the knight?
23. There is a vending machine located outside the hallway door to the back of the building. Determine the price per soda or water, and the number of flavors. What coin or bill combinations may be used to purchase one, two, three, or four cans of soda?

Part 5: Outside

24. At the flagpole on the front of the school, measure the length and height of an exterior wall brick. Measure from the beginning of one brick to the beginning of the next brick. Count the number of bricks from the ground to the metal flashing. Estimate the height of the building.
25. Repeat the process given in problem 24 while standing by the G24 Storage marker, near the Children's Center play area. Estimate the average height per story of the school.
26. Locate the concentric concrete circles near the Children's Center play area. Measure the diameter of the inner circle and the width of the annulus. Find the area of the outer circle, the inner circle, and one section of the annulus.
27. There is a circular parking lot at the south end of the school, outside of the Children's Center. Find the following:
 - a. Estimate the number of degrees of a circle through which there are painted parking spots.
 - b. Count the number of parking spots. Count the half-sized handicapped access spot (blue-striped) as one-half of a spot.
 - c. Calculate the number of degrees per parking spot.
28. In the circular parking lot, use the following measurements: radius of the grassy circle, $17\frac{1}{2}$ feet; 34 feet from the curb to the back end of the parking stripe; and length of the parking stripe, $17\frac{1}{2}$ feet. Calculate the largest and smallest widths of a parking spot. Compare these to actual measurements.

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29. In the circular parking lot, consider a parking spot to be a trapezoid. Find the area of the parking spot. (Use approximate values.)
30. Locate the outside staircase on the west side of the school (facing UTC Place). Measure the rise and run of a step. Calculate the slope of the staircase. Repeat for another step. Repeat for an inside staircase in the main hallway. Which staircase has more uniform steps? State a reason for your selection.
31. In either school parking lot, count the following: total number of cars, cars with a Tennessee license plate, cars with an out-of-state license plate, cars with a specialty license plate (for example, Animal Friendly), and cars with a personalized license plate. Find the following:
- The ratio of Tennessee to out-of-state license plates (all types).
 - The ratio of specialty to traditional license plates (all states).
 - The percentage of Tennessee license plates (all types).
 - The percentage of out-of-state license plates (all types).
 - The percentage of personalized license plates.
 - The number of possible license plate combinations for a traditional Tennessee license plate.
 - The number of possible license plate combinations for a specialty Tennessee license plate (if present).
 - The number of possible license plate combinations for a traditional out-of-state license plate (if present). List the name of the state.
 - In what way or ways are traditional and specialty license plates similar?
 - In what way or ways are traditional and specialty license plates different?
 - The number of possible license plate combinations for a personalized Tennessee license plate (minimum of three numbers and/or letters, maximum of seven numbers and/or letters).
 - Design a personalized Tennessee license plate for yourself.

Solutions

Part 1: Library

1. The bookshelf that holds Encyclopedia Britannica is 35 inches wide. Each volume of the encyclopedia is 1 ½ inches wide (across the binding). The bottom shelf contains 22 volumes. Is there space for additional volumes? If so, how many?

$22 \text{ volumes} \times 1.5 \text{ in./volume} = 33 \text{ in.}$
 $35 \text{ in.} - 33 \text{ in.} = 2 \text{ in.}$
 $2 \text{ in.} \div 1.5 \text{ in./volume} = 1.33 \text{ volumes}$
 There is space for 1 additional volume.

2. The fiction books range in height from 7 inches to 11 inches. The bookcase that contains fiction is 54 inches tall. There are 39 shelving holes with 1 ¼-inch spacing between them. The shelf is ¾-inch thick. Design an arrangement for the shelving.

Answers will vary. One possible arrangement: 12 1/2 inches of clearance from the bottom shelf, place pins at the 10th set of holes (12 1/2 inches), ¾-inch shelf, 11 3/4 inches of clearance, place pins at the 20th set of holes (25 inches), ¾-inch shelf, 9 1/4 inches of clearance, place pins at the 28th set of holes (35 inches), ¾-inch shelf, 9 1/4 inches of clearance, place pins at the 36th set of holes (45 inches), ¾-inch shelf, 8 1/4 inches of clearance.

3. The width (across the binding) of fiction books ranges from ½ inch to 1 inch. The bookshelf is 35 inches wide. What is the minimum number of books that will fill the shelf? What is the maximum number of books that will fill the shelf?

Minimum: $35 \text{ in.} \div 1 \text{ in./book} = 35 \text{ books}$
 Maximum: $35 \text{ in.} \div 0.5 \text{ in./book} = 70 \text{ books}$

4. The magazine rack tilts to display the cover of the latest issue of each magazine. What is the slope of the tilted surface if the depth of the case is 1 foot and the height of the case is 10 inches?

Slope = rise / run
 Slope = $10 \text{ in.} / (1 \text{ ft} \times 12 \text{ in./ft}) = 10/12 = 5/6$

5. The library contains square tables and round tables. Each square table has sides of length 42 inches. Each round table has a diameter of 41 inches. Find the surface area of each type of table.

Square: $42 \text{ in.} \times 42 \text{ in.} = 1,764 \text{ in.}^2$
 $1,764 \text{ in.}^2 \times 1 \text{ ft}^2/144 \text{ in.}^2 = 12.25 \text{ ft}^2$

Circle: $\Pi r^2 = 3.14 \times (41 \text{ in.}/2)^2 = 1,320 \text{ in.}^2$
 $1,320 \text{ in.}^2 \times 1 \text{ ft}^2/144 \text{ in.}^2 = 9.17 \text{ ft}^2$

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Part 2: Gymnasium

6. The gymnasium floor contains markings for a basketball court. Describe the lines, angles, and symmetry that can be seen.

Answers will vary. Answers should include sightings of right angles, parallel lines, perpendicular lines, mirror symmetry (reflection), rotational symmetry (through 180°), etc.

7. Given the full court (NBA/NCAA) diagram (Handymanwire, 2003), find the following:
- a. The ratio of the length of the court (94 ft) to the width of the court (50 ft).

$$94 \text{ ft} \div 50 \text{ ft} = 1.88$$

- b. The area of the backboard (72 inches in width by 42 inches in height).

$$\begin{aligned} \text{Area} &= 72 \text{ in.} \times 42 \text{ in.} = 3,024 \text{ in.}^2 \\ 3,024 \text{ in.}^2 \times 1 \text{ ft}^2/144 \text{ in.}^2 &= 6 \text{ ft}^2 \end{aligned}$$

- c. The area of the key (12 ft wide, 15 ft from free throw line to backboard, 4 ft from backboard to baseline). Don't forget the semicircle at the top of the key!

$$\begin{aligned} \text{Rectangle: Area} &= 12 \text{ ft} \times (15 \text{ ft} + 4 \text{ ft}) = 12 \text{ ft} \times 19 \text{ ft} = 228 \text{ ft}^2 \\ \text{Semicircle: Area} &= \Pi r^2/2 = [3.14 \times (6 \text{ ft})^2] / 2 = 56.52 \text{ ft}^2 \\ \text{Total: } 228 \text{ ft}^2 + 56.52 \text{ ft}^2 &= 284.52 \text{ ft}^2 \end{aligned}$$

- d. The area of the rim (18 inches in diameter).

$$\begin{aligned} \text{Area} &= \Pi r^2; r = d/2 \\ \text{Area} &= 3.14 \times (9 \text{ in.})^2 = 254.35 \text{ in.}^2 \end{aligned}$$

- e. The circumference of the rim (18 inches in diameter).

$$\text{Circumference} = 2\Pi r = \Pi d = 3.14 \times 18 \text{ in.} = 56.52 \text{ in.}^2$$

- f. The circumference of an NBA basketball is 29.5 inches. How many inches clearance does the basketball have as it passes through the rim?

$$\begin{aligned} d &= C/\Pi = 29.5 \text{ in.} / 3.14 = 9.4 \text{ in.} \\ 18 \text{ in.} - 9.4 \text{ in.} &= 8.6 \text{ in.} \text{ (about 4.3 in. around the inner edge)} \end{aligned}$$

- g. The volume of an NBA basketball.

$$\text{Volume} = (4/3)\Pi r^3 = (4/3) \times 3.14 \times (4.7 \text{ in.})^3 = 435 \text{ in.}^3$$

- h. The length of the hypotenuse of the right triangle formed by the distance from the free throw line to the backboard (15 ft) and the distance from the floor to the rim of the basket (10 ft).

$$c^2 = a^2 + b^2$$

$$c^2 = (15 \text{ ft})^2 + (10 \text{ ft})^2 = 225 \text{ ft}^2 + 100 \text{ ft}^2 = 325 \text{ ft}^2$$

$$c = 18 \text{ ft}$$

Part 3: Cafeteria

8. The wall is composed of 8-inch blocks. Find the height of the wall.

$$8 \text{ in./block} \times 16 \text{ blocks} = 128 \text{ in.} = 10.67 \text{ ft.}$$

9. Each cafeteria table has a length of 95 ½ inches, a table width of 14 ½ inches, and a bench width of 11 ½ inches. Find the surface area of the table and the bench (top surface only).

$$\text{Area of table} = 95.5 \text{ in.} \times 14.5 \text{ in.} = 1,384.75 \text{ in.}^2 = 9.6 \text{ ft}^2$$

$$\text{Area of bench} = 95.5 \text{ in.} \times 11.5 \text{ in.} = 1,098.25 \text{ in.}^2 = 7.6 \text{ ft}^2$$

10. Estimate the following:

- a. The number of adults that can sit side-by-side on the bench.

$$95.5 \text{ in.} \div 20 \text{ in./adult} = 4.775 \text{ adults, or about 4 or 5 adults}$$

- b. The number of students that can sit side-by-side on the bench.

$$95.5 \text{ in.} \div 15 \text{ in./child} = 6.367 \text{ children, or about 6 or 7 children}$$

- c. If there are 45 tables, how many students can be seated at the same time?

$$45 \text{ tables} \times 6 \text{ children/table} = 270 \text{ children}$$

$$45 \text{ tables} \times 7 \text{ children/table} = 315 \text{ children}$$

A range of 270 to 300 children is a good estimate.

11. Count the number of 1-foot tiles along the length and width of the floor. Calculate the area of the floor in square feet and in square yards. Consider only full tiles.

Floor is 48 ft by 78 ft (16 yards by 26 yards).

$$\text{Area} = 48 \text{ ft} \times 78 \text{ ft} = 3,744 \text{ ft}^2$$

$$\text{Area} = 16 \text{ yd} \times 26 \text{ yd} = 416 \text{ yd}^2$$

12. Count the number of 4-foot by 2-foot panels along the length and width of the ceiling. Calculate the area of the ceiling in square feet and in square yards. Consider only full panels.

19 panels long (4 ft) by 24 panels across (2 ft).
 One panel is 8 ft², so (19 x 24) panels are 3,648 ft².
 $3,648 \text{ ft}^2 \times 1 \text{ yd}^2/9 \text{ ft}^2 = 405.3 \text{ yd}^2$

13. Compare the results obtained in problems 11 and 12 by calculating the percent error between the two measurements. Both values are based on observations, but the length as counted in floor tiles will be more accurate since this is a smaller unit. Use the area calculated with floor tiles as the accepted value and the area calculated with ceiling panels as the observed value.

Percent error = $\left[\frac{(\text{observed} - \text{accepted})}{\text{accepted}} \right] \times 100\%$
 $= \left[\frac{(405.3 \text{ yd}^2 - 416 \text{ yd}^2)}{416 \text{ yd}^2} \right] \times 100\%$
 $= \left[\frac{(-10.7 \text{ in.} / 416 \text{ yd}^2)}{1} \right] \times 100\%$
 $= 0.0257 \times 100\%$
 $= 2.57\%$

14. Using the data collected in problems 8 and 11, calculate the volume of the room. Count the number of 2-foot diffusers and the number of 2-foot by 1-foot uptake vents in the ceiling. What volume of air is changed per diffuser and per uptake vent? Assume two room changes of air per hour. Express your answers in cubic feet per minute (cfm).

Volume = $10.67 \text{ ft} \times 3,744 \text{ ft}^2 = 39,948 \text{ ft}^3$
 Diffusers: 8; Uptake vents: 4
 Diffuser: $39,948 \text{ ft}^3 \times 2/\text{hr} \times 1 \text{ hr}/60 \text{ min} \div 8 = 166 \text{ ft}^3/\text{min} \text{ (cfm)}$
 Uptake vent: $39,948 \text{ ft}^3 \times 2/\text{hr} \times 1 \text{ hr}/60 \text{ min} \div 4 = 333 \text{ ft}^3/\text{min} \text{ (cfm)}$

15. Count the number of 4-foot by 2-foot light panels in the ceiling. Calculate the percentage of the ceiling that has light panels.

$35 \text{ panels} \div 456 \text{ panels} = 0.077$
 $0.077 \times 100\% = 7.7\%$

16. Count the number of sprinkler heads in the ceiling. Calculate the percentage of the ceiling panels that contain a sprinkler head.

$28 \text{ panels} \div 456 \text{ panels} = 0.061$
 $0.061 \times 100\% = 6.1\%$

17. Draw a scale of the room. Construct the minimum size of the sprinkler head spray radius to obtain complete coverage of the floor.

Answers will vary. Hint: Simulate with circles, or outlines of round objects, for example, drawing the outlines of the bottoms of four soda cans.

18. Locate a nine-pane window. How many different sizes of panes are present? What is the ratio of the smallest pane to the largest pane?

There are six sizes of window panes present, since the left and right columns contain the same sized panes.

Smallest: 11.5 in. x 27.5 in. = 316.25 in.²

Largest: 36 in. x 30 in. = 1,080 in.²

Ratio: $316.25 \text{ in.}^2 \div 1,080 \text{ in.}^2 = 0.29$ (or between $\frac{1}{4}$ and $\frac{1}{3}$ as large)

Part 4: Connections

19. Look for patterns in the hallway and/or room floor tiles, on the walls, etc. Where can you find examples of odd numbers, even numbers, and/or prime numbers?

Answers will vary. Number patterns present include groups of 5 and 13 in cafeteria floor tiles, 9 tiles per dark tile area, exterior brick work includes 11 groups of 3 vertical bricks as a unit, cafeteria exterior includes 5 groups of 3 vertical bricks as a unit, odd or even numbers can be seen in the hallway floor tiles, etc.

20. Look at the murals in the hallway, across from the school office. List the following:
- Geometric shapes that you see.

Answers will vary. Examples: square, circle, triangle, six-sided star, etc.

- Repeated patterns that you see.

Answers will vary. Examples: feathers/leaves, rectangles, etc.

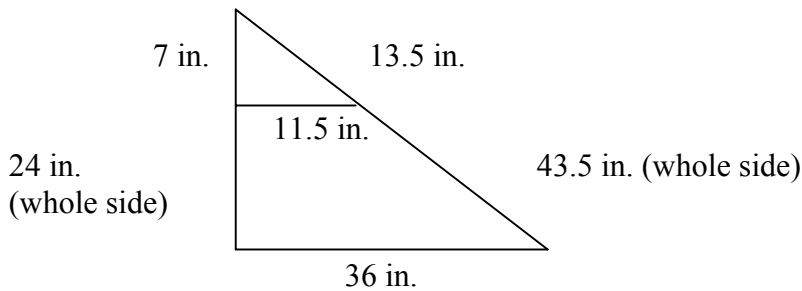
- Types of symmetry that you see.

Answers will vary. Examples: reflection, rotation, translation.

- List the time periods and locations that you see.

Answers will vary. Time periods: Ancient Egypt, Ancient Greece, Roman Empire, Medieval/Renaissance, Modern. Locations: Egypt, Greece, Rome, Genoa, Moors/Africa, Japan, Aztec/Central America, Native American/Southwest/Southeast/etc., Chattanooga.

21. Look at the left or right side of the roof of the Tennessee Aquarium model. Measure the three sides of the large and small triangles. Show that they are similar.



Show that the ratios of the sides are the same for the small and large triangles:

$$24 \text{ in.} \div 7 \text{ in.} = 3.43$$

$$36 \text{ in.} \div 11.5 \text{ in.} = 3.13$$

$$43.5 \text{ in.} \div 13.5 \text{ in.} = 3.22$$

22. Measure the height of the knight sculpture. What percentage of your height is the knight?

The knight is 43 in. tall. I am 60 in. tall.

$$43 \text{ in.} \div 60 \text{ in.} = 0.72$$

$$0.72 \times 100\% = 72\%$$

23. There is a vending machine located outside the hallway door to the back of the building. Determine the price per soda or water, and the number of flavors. What coin or bill combinations may be used to purchase one, two, three, or four cans of soda?

Answers will vary. There are 7 flavors, and the cost is 60 cents per can. The vending machine accepts quarters, dimes, nickels, and dollar bills. Example: Four cans of soda could be purchased with two dollar bills, one quarter, one dime, and one nickel. (The machine may provide change in between purchases.)

Part 5: Outside

24. At the flagpole on the front of the school, measure the length and height of an exterior wall brick. Measure from the beginning of one brick to the beginning of the next brick. Count the number of bricks from the ground to the metal flashing. Estimate the height of the building.

Dimensions of the brick: 8.25 in. by 2.75 in.

By the flagpole: 12 red, 3 yellow, 17 red, 3 yellow, 3 red 51 yellow, yellow vertical, 3 red, 15 yellow. Total of 105 horizontal (2.75 in.) and 1 row vertical (8.25 in.)

$$(105 \times 2.75 \text{ in.}) + (1 \times 8.25 \text{ in.}) = 288.75 \text{ in.} + 8.25 \text{ in.} = 297 \text{ in.}$$

$$297 \text{ in.} \times 1 \text{ ft}/12 \text{ in.} = 24.75 \text{ ft}$$

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25. Repeat the process given in problem 24 while standing by the G24 Storage marker, near the Children's Center play area. Estimate the average height per story of the school.

Dimensions of the brick: 8.25 in. by 2.75 in.

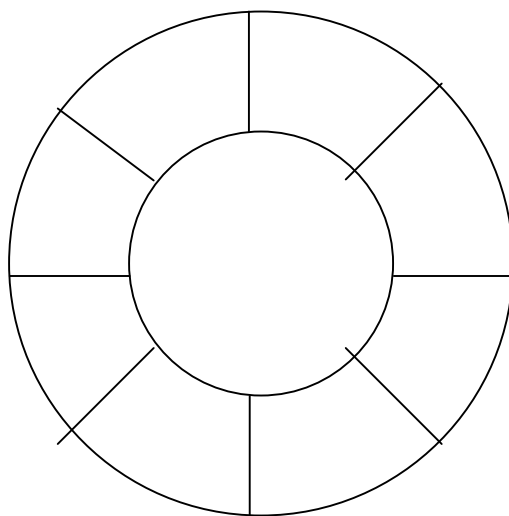
By G24 storage: 29 red, 3 yellow, 36 red, 3 yellow, 20 red 3 yellow, 3 red, 49 yellow, yellow vertical, 18 yellow. Total of 164 horizontal (2.75 in.) and 1 row vertical (8.25 in.)

$$(164 \times 2.75 \text{ in.}) + (1 \times 8.25 \text{ in.}) = 451 \text{ in.} + 8.25 \text{ in.} = 459.25 \text{ in.}$$

$$459.25 \text{ in.} \times 1 \text{ ft}/12 \text{ in.} = 38.27 \text{ ft}$$

$$38.27 \text{ ft} \div 3 \text{ stories} = 12.76 \text{ ft/story}$$

26. Locate the concentric concrete circles near the Children's Center play area. Measure the diameter of the inner circle and the width of the annulus. Find the area of the outer circle, the inner circle, and one section of the annulus.



Diameter of inner circle: 117 in.

Spoke: 59 in.

$$\begin{aligned} \text{Area of outer circle: } \pi r^2 \\ &= 3.14 \times (117.5 \text{ in.})^2 \\ &= 43,352 \text{ in.}^2 = 301 \text{ ft}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of inner circle: } \pi r^2 \\ &= 3.14 \times (58.5 \text{ in.})^2 \\ &= 10,746 \text{ in.}^2 = 75 \text{ ft}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of annulus section:} \\ &= (\text{outer area} - \text{inner area}) / 8 \\ &= (301 \text{ ft}^2 - 75 \text{ ft}^2) / 8 = 28.25 \text{ ft}^2 \end{aligned}$$

27. There is a circular parking lot at the south end of the school, outside of the Children's Center. Find the following:

- a. Estimate the number of degrees of a circle through which there are painted parking spots.

$$\frac{3}{4} \text{ of a circle, or } 270^\circ$$

- b. Count the number of parking spots. Count the half-sized handicapped access spot (blue-striped) as one-half of a spot.

There are 27 parking spots.

- c. Calculate the number of degrees per parking spot.

$$270^\circ \div 27 \text{ parking spots} = 10^\circ / \text{parking spot}$$

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28. In the circular parking lot, use the following measurements: radius of the grassy circle, $17\frac{1}{2}$ feet; 34 feet from the curb to the back end of the parking stripe; and length of the parking stripe, $17\frac{1}{2}$ feet. Calculate the largest and smallest widths of a parking spot. Compare these to actual measurements.

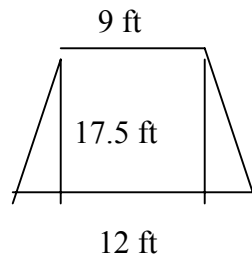
$$\text{Circumference of the large circle} = 2\pi r = 2 \times 3.14 \times 69 \text{ ft} = 433 \text{ ft}$$

$$\text{Circumference of the circle at back end of stripe} = 2\pi r = 2 \times 3.14 \times 51.5 \text{ ft} = 323 \text{ ft}$$

$$\text{Calculated: } 433 \text{ ft} \div 36 = 12.03 \text{ ft} \quad \text{Observed: } 15.2 \text{ ft} \quad \text{Percent error: } 26\%$$

$$\text{Calculated: } 323 \text{ ft} \div 36 = 8.97 \text{ ft} \quad \text{Observed: } 11.5 \text{ ft} \quad \text{Percent error: } 28\%$$

29. In the circular parking lot, consider a parking spot to be a trapezoid. Find the area of the parking spot. (Use approximate values.)



$$\begin{aligned} \text{Area} &= (1/2)(h)(b_1 + b_2) \\ &= 0.5 \times 17.5 \text{ ft} \times (9 \text{ ft} + 12 \text{ ft}) \\ &= 183.75 \text{ ft}^2 \end{aligned}$$

30. Locate the outside staircase on the west side of the school (facing UTC Place). Measure the rise and run of a step. Calculate the slope of the staircase. Repeat for another step. Repeat for an inside staircase in the main hallway. Which staircase has more uniform steps? State a reason for your selection.

$$\text{Concrete: rise/run} = 6.5 \text{ in.} / 11 \text{ in.} = 0.59 \text{ (not uniform)}$$

$$\text{Inside staircase: rise/run} = 7 \text{ in.} / 10.5 \text{ in.} = 0.67 \text{ (uniform)}$$

The inside staircase is made from uniform metal pieces; the concrete was poured for each individual step.

31. In either school parking lot, count the following: total number of cars, cars with a Tennessee license plate, cars with an out-of-state license plate, cars with a specialty license plate (for example, Animal Friendly), and cars with a personalized license plate. Find the following:
- The ratio of Tennessee to out-of-state license plates (all types).
 - The ratio of specialty to traditional license plates (all states).
 - The percentage of Tennessee license plates (all types).
 - The percentage of out-of-state license plates (all types).
 - The percentage of personalized license plates.

Answers will vary for 31a – 31 e, depending on the parking lot selected and the cars parked in the given lot.

- f. The number of possible license plate combinations for a traditional Tennessee license plate.

Example: BEY 731 (3 letters, 3 numbers)
 $26 \times 26 \times 26 \times 10 \times 10 \times 10 = 17,576,000$

- g. The number of possible license plate combinations for a specialty Tennessee license plate (if present).

Example: AN 0000 (AN is the code for Animal Friendly)
 $10 \times 10 \times 10 \times 10 = 10,000$ (for each type of specialty plate)

- h. The number of possible license plate combinations for a traditional out-of-state license plate (if present). List the name of the state.

Answers will vary. Example: Massachusetts license plates have 3 numbers followed by 3 letters. The number of combinations would be the same as for Tennessee.

- i. In what way or ways are traditional and specialty license plates similar?

Answers will vary. Example: They both contain numbers.

- j. In what way or ways are traditional and specialty license plates different?

Answers will vary. Example: Specialty plates contain only numbers.

- k. The number of possible license plate combinations for a personalized Tennessee license plate (minimum of three numbers and/or letters, maximum of seven numbers and/or letters).

Total letters and numbers: $26 + 10 = 36$

$$36^3 = 46,656 \quad 36^4 = 1,679,616 \quad 36^5 = 60,466,176$$

$$36^6 = 2,176,782,336 \text{ (subtract traditional plates)}$$

$$2,176,782,336 - 17,576,000 = 2,159,206,336$$

$$36^7 = 78,364,164,096$$

$$\text{Total} = 80,585,562,880 \text{ (over 80 billion)}$$

- l. Design a personalized Tennessee license plate for yourself.

DEBORAH SP2 TNTUX00

Reference

Handymanwire. (2003). *Basketball courts*. Retrieved July 19, 2003, from <http://www.handymanwire.com/articles/basketballcourt.html>. This diagram is also located at <http://www.hoopinc.com/pages/dimensions/dimensions.html>, http://www.basketballgoals.com/basketball_court_dimensions_new.html, and possibly other Web sites. (Ownership of the diagram is unclear.)

Web Sites for Further Exploration

Dr. Tommie F. Brown Academy for Classical Studies
http://www.hcde.org/schools/elementary/brown_academy/hcde_default.html

Math Forum Geometry Problem of the Week: Play Ball! (February 14, 2000)
<http://mathforum.org/geopow/solutions/solution.ehtml?puzzle=66>

Department of Safety – Specialty License Plates
<http://www.tennessee.gov/safety/plates.html>

U.S. License Plates 1969 – Present
<http://www.15q.net/usindex.html>

License Plates of American Indian Tribes
<http://www.pl8s.com/tribals/indians.htm>

HyperHistory Online
http://www.hyperhistory.com/online_n2/History_n2/a.html

Annulus – from MathWorld
<http://mathworld.wolfram.com/Annulus.html>

The Annulus Calculator
<http://www.ex.ac.uk/cimt/res2/calcs/calannu.htm>

The Prime Pages
<http://www.utm.edu/research/primes/>

Geometric Shapes and Figures
<http://www.washburn.k12.il.us/severinsen/geometry.htm>

Knights and Armor
<http://www.knightsandarmor.com/>

Ask Dr. Math: Degrees in a Circle
<http://mathforum.org/library/drmath/view/58395.html>